

Table 1. Calculated values of radial, circumferential and shear stresses developed in the matrix for the cases of cavity, rigid and elastic inclusion upon subjection to external hydrostatic pressure

Case	Reference	$\sigma_{rr}$ in matrix	$\sigma_{\theta\theta}$ in matrix ( $=\sigma_{\phi\phi}$ )	Absolute value of $\tau_{\max}$ (at $r=a$ ) in matrix
I. Cavity (a) Zero internal pressure (b) Internal pressure ( $-P_i$ ) only (c) Internal pressure ( $-P_i$ ) and external pressure ( $-P$ )	Present calculation	$-P(1-a^3/r^3)$	$-P[1+1/2(a/r)^3]$	$3/4 P$
	Present calculation	$-P_i(a/r)^3$	$P_i/2(a/r)^3$	$3/4 P_i$
	Present calculation	$-P+(P-P_i)\frac{a^3}{r^3}$	$-P-(P-P_i)\frac{a^3}{2r^3}$	$3/4 (P-P_i)$
II. Rigid inclusion	Hahn and Rosenfield's (1966) equation	—	—	$\approx P/3$
	Present calculation	$-P \left[ 1 + \frac{2(1-2\nu)}{1+\nu} \cdot (a/r)^3 \right]$	$-P \left[ 1 - \frac{1-2\nu}{1+\nu} \cdot (a/r)^3 \right]$	$(G/K) \cdot P$
III. Elastic inclusion	Hahn and Rosenfield (1966)	—	—	$(P/3) \left[ \frac{(K-K_i)}{K_i} \right]^\dagger$
	Present calculation	$-P \frac{3E_i(1-\nu)}{(1+\nu)E_i+2(1-2\nu_i)E}$ at $r=a$	$-P \frac{3\nu E_i+3(1-2\nu_i)E}{(1+\nu)E_i+2(1-2\nu_i)E}$ at $r=a$	$\frac{3PG}{K} \left[ \frac{K-K_i}{3K_i+4G} \right]$

† Note:  $\tau_{\max}$  in Hahn and Rosenfield's equation goes to infinity as  $K_i \rightarrow 0$ .

$-P$ : External hydrostatic pressure,  
 $\nu, \nu_i$ : Poisson's ratio of the matrix  
 and inclusion, respectively,  
 $K, K_i$ : Bulk modulus of the matrix  
 and inclusion, respectively,

$(-P_i)$ : Internal pressure,  
 $r$ : Radius vector,  
 $\tau_{\max}$ : Maximum shear stress,  
 $\sigma_{rr}, \sigma_{\theta\theta}, \sigma_{\phi\phi}$ : Radial, circumferential and  
 azimuthal stress, respectively,

$a$ : The radius of the inclusion,  
 $G$ : Shear modulus of the matrix,  
 $E, E_i$ : Young's modulus of the matrix  
 and inclusion, respectively.

Table 2. Calculated stress  $\tau_{\max}$  at spherical cavity, rigid and elastic inclusion in copper matrix as a function of the applied hydrostatic pressure

$\tau_{\max}$ (p.s.i.)	Elastic inclusion†